

Third Romanian Itinerant Seminar on
Mathematical Analysis and its Applications

Alba Iulia, September 10-12, 2021

Edited by:

- Ioan-Lucian Popa ("1 Decembrie 1918" University of Alba Iulia)
- Daniel Breaz ("1 Decembrie 1918" University of Alba Iulia)

Contents

Opening Speech	1
Technical Program	3
Abstracts	7
Some new trends in fractional calculus and its applications (<i>Dumitru Băleanu</i>)	7
Fixed Point Equations with Abstract Volterra Operators on Spaces of Functions of Several Variables (<i>Adrian Petruşel</i>)	7
On Some Concepts of Uniform Dichotomy for Evolution Operators in Banach Spaces (<i>Rovana Boruga(Toma), Mihail Megan, Daniela Maria-Magdalena Toth</i>)	8
Recent Trends in Geometric Function Theory (<i>Daniel Breaz</i>)	8
Convergence Estimates for Some Two Parameters Singularly Perturbed Problems for Sine-Gordon Type Equations (<i>Andrei Perjan, Galina Rusu</i>)	9
On Well-posedness Associated With a New Class of Constrained Optimization Problems (<i>Savin Treanţă</i>)	10
A Spectral Criterion for the Existence of the Stabilizing Solution of a Class of Riccati Type Differential Equations with Periodic Coefficients (<i>Vasile Drăgan, Ioan-Lucian Popa</i>)	10
On A_n -bounded Operator Valued Analytic Functions (<i>Ilie Valuşescu</i>)	11
Adaptive Gradient Descent and Slow Manifolds (<i>Adrian Viorel</i>)	11
On Some Exact Integral Formulae for Polynomial Coefficients and Enumeration of Multipartitions (<i>Ovidiu Bagdasar</i>)	12
The Determinant Formulae for the Rodrigues General Problem when the Eigenvalues Have Double Multiplicity (<i>Dorin Andrica, Oana-Liliana Chender</i>)	12
A Fractional Differential Inclusion with Mixed Boundary Conditions (<i>Aurelian Cernea</i>)	13
The Hardy-Littlewood-Pólya Inequality of Majorization in the Context of Ordered Banach Spaces (<i>Constantin P. Niculescu</i>)	14
Numerical Probabilistic Analysis of a Generalized Random Logistic Model (<i>Vicente Bevia, Juan Carlos Cortés</i>)	14
On Some Concepts of Uniform Dichotomy for Evolution Operators in Banach Spaces (<i>Timea Melinda Szemely Fülöp, Ariana Găină, Carmen Florinela Popa</i>)	15

Maia's Fixed Point Theorems for Discontinuous Mappings (<i>Paula Mihaela Tamara Homorodan</i>)	15
Torsional Creep Problems Involving Grushin p -Laplacian (<i>Denisa Stancu-Dumitru</i>)	16
On Coupled Nonlinear Oscillators of a Mechanical System of Vibration Reduction (<i>Gheorghe Moroşanu, Cristian Vladimirescu</i>)	16
Dynamics of the Infection by SARS-CoV-2 (<i>Carla M.A. Pinto</i>)	17
Unbounded Solutions of Third Order Three-point Boundary Value Problems on a Half-line (<i>Ravi P. Agarwal</i>)	17
Author Index	19

Opening Speech

by Professor Gheorghe Morosanu
(Babes-Bolyai University)

Dear Colleagues,

Welcome to the third meeting of the Romanian Itinerant Seminar on Mathematical Analysis and Its Applications (RISMAA) that I launched myself in 2017.

As you know, the first meeting took place in 2018 at Babes-Bolyai University, the organizers being then Professors Adrian Petrusel, Marcel Serban and myself. It was a very successful conference, which strengthened our hope for a remarkable future evolution of this scientific project.

The second edition of RISMAA took place in 2019 at the Ovidius University of Constanta, under the coordination of the late Professor Constantin Popa. It was also a great success which confirmed the need for these periodic meetings of researchers who love mathematical analysis. I myself participated then, with great enthusiasm, and I gave a plenary lecture on that occasion. At the end of that conference, our colleague Lucian Popa came to me, on his own initiative, and told me that he wanted to organize the third meeting, in 2020, at the University of Alba Iulia. Unfortunately, the covid pandemic strongly influenced his plan from bad to worse. I recall that when I launched RISMAA (in 2017), I stated that *although there are nowadays excellent means of communication, face-to-face conversations cannot be replaced by anything else, so periodic meetings are strongly needed.*

By meetings I then meant meetings in person. Under the present circumstances we cannot completely follow this idea. It was decided to postpone the third edition of RISMAA for 2021, and replace the live format with the hybrid format.

I apologize that I myself cannot participate in person at this edition of RISMAA. Part of my family lives in the US and I have not been able to get there in the last 2 years. My grandchildren's invitation was stronger than my desire to meet you. But I am with you from afar and I will try to follow online what is going to happen in Alba Iulia.

I wish you all Good Luck! See you at the next edition of RISMAA!

Conference via Zoom:

Time: Sep 10, 2021 17:00 PM Bucharest

Join Zoom Meeting:

<https://zoom.us/j/4103568066?pwd=d2hOQkR4STdkL0NEUkFBWEhiaUNrUT09>

Meeting ID: 410 356 8066

Passcode: RISMAA-21

Time: Sep 11, 2021 9:00 AM Bucharest

Join Zoom Meeting:

<https://zoom.us/j/4103568066?pwd=d2hOQkR4STdkL0NEUkFBWEhiaUNrUT09>

Meeting ID: 410 356 8066

Passcode: RISMAA-21

Technical Program

September 10, 2021

16:00 - 17:00 Registration. Venue: Apor Palace

17:00 - 17:20 Opening Session (Council Hall)

Opening Address

Prof. Dr. Daniel Breaz

Rector of "1 Decembrie 1918" University of Alba Iulia

17:20-19:00 Session 1 (Council Hall) Chair: Constantin P. Niculescu

17:20-18:00 Some New Trends in Fractional Calculus and its Applications

Dumitru Băleanu

18:00-18:40 Fixed Point Equations with Abstract Volterra Operators on Spaces of Functions of Several Variables

Adrian Petrușel

18:40-19:00 On Some Concepts of Uniform Dichotomy for Evolution Operators in Banach Spaces

Rovana Boruga(Toma), Mihail Megan, Daniela Maria-Magdalena Toth

19:00-21:00 Welcome Reception (University Restaurant)

September 11, 2021

9:00-11:00 Session 2 (Council Hall) Chair: Dorin Andrica

9:00-9:40 Recent Trends in Geometric Function Theory

Daniel Breaz

9:40-10:00 Convergence Estimates for Some Two Parameters Singularly Perturbed Problems for Sine-Gordon Type Equations

Andrei Perjan, Galina Rusu

- 10:00-10:20 On Well-posedness Associated with a New Class of Constrained Optimization Problems
Savin Treanță
- 10:20-10:40 A Spectral Criterion for the Existence of the Stabilizing Solution of a Class of Riccati Type Differential Equations with Periodic Coefficients
Vasile Drăgan, Ioan-Lucian Popa
- 10:40-11:00 On A_n -Bounded Operator Valued Analytic Functions
Ilie Valușescu

11:00-11:30 Coffee Break

11:30-12:40 Session 3 (Council Hall) Chair: Ilie Valușescu

- 11:30-11:50 Adaptive Gradient Descent and Slow Manifolds
Adrian Viorel
- 11:50-12:10 Cauchy's Integral Formula with Applications to Polynomial Coefficients and Partitions
Ovidiu Bagdasar
- 12:10-12:30 The Determinant Formulae for the Rodrigues General Problem When the Eigenvalues Have Double Multiplicity
Dorin Andrica, Oana-Liliana Chender
- 12:30-12:50 A Fractional Differential Inclusion with Mixed Boundary Conditions
Aurelian Cernea

12:50 - 14:00 Lunch (University Restaurant)

14:00-17:20 Session 4 (Council Hall) Chair: Aurelian Cernea

- 14:00-14:40 The Hardy-Littlewood-Pólya Inequality of Majorization in the Context of Ordered Banach Spaces
Constantin P. Niculescu
- 14:40-15:00 Numerical Probabilistic Analysis of a Generalized Random Logistic Model
Vicente Bevia, Juan Carlos Cortés
- 15:00-15:20 On Uniform Stability of Linear Discrete-time Systems in Banach Spaces
Timea Melinda Szemely Fülöp, Ariana Găină, Carmen Florinela Popa
- 15:20-15:40 Maia's Fixed Point Theorems for Discontinuous Mappings
Paula Mihaela Tamara Homorodan

- 15:40-16:00 Torsional Creep Problems Involving Grushin p -Laplacian
Denisa Stancu-Dumitru
- 16:00-16:20 On Coupled Nonlinear Oscillators of a Mechanical System
of Vibration Reduction
Gheorghe Moroşanu, Cristian Vladimirescu
- 16:20-16:40 Dynamics of the Infection by SARS-CoV-2
Carla M.A. Pinto
- 16:40-17:20 Unbounded Solutions of Third Order Three-point Boundary
Value Problems on a Half-line
Ravi P. Agarwal
- 17:20-19:00 Tour of Alba Iulia Citadel**
- 19:00-21:00 Dinner (University Restaurant)**

September 12, 2021

Departure of participants

Abstracts

Some new trends in fractional calculus and its applications

Sep 10
17:20-18:00

Dumitru Băleanu¹

¹Department of Mathematics, Faculty of Art and Sciences, Cankaya University, Ankara, Turkey

²Institute of Space Sciences, Magurele-Bucharest, Romania

Abstract: Fractional calculus deals with the study of the fractional-order integral and derivative operators over real or complex domains, and their applications. In my talk, I will present some new trends from both theoretical and experimental viewpoints.

Fixed Point Equations with Abstract Volterra Operators on Spaces of Functions of Several Variables

Sep 10
18:00-18:40

Adrian Petruşel¹

¹Babeş-Bolyai University Cluj-Napoca, Romania

Abstract: Several notions of abstract Volterra operators on spaces of functions of one variable are well known (C. Corduneanu, Abstract Volterra equations: a survey, Math. Comput. Modeling, 32(2000), 1503-1528; E.S. Zhukovskii, M.J. Alves, Abstract Volterra operators, Russian Math., 52(2008), No. 3, 1-14; I.A. Rus, Some variants of contraction principle in the case of operators with Volterra property: step by step contraction principle, Adv. Theory of Nonlinear Anal. Appl., 3(2019), No. 3, 111-120). In this paper, we introduce various notions of abstract Volterra operators in spaces of functions of several variables. Some fixed point equations with such abstract Volterra operators are also studied. The basic ingredient in the theory of step by step contraction is the notion of G-contraction (I.A. Rus, Cyclic representations and fixed points, Annals T. Popoviciu Seminar, 3(2005), 171-178). The relevance of step by step contraction principle is illustrated by applications in the theory of Darboux-Ionescu problem.

The talk is based on some recent joint works with I.A. Rus and M.A. Şerban.

References:

[1] T.A. Burton: *A note on existence and uniqueness for integral equations with sum of two operators: progressive contractions*, Fixed Point Theory, **20**(2019), no. 1, 107-113.

- [2] C. Corduneanu: *Abstract Volterra equations: a survey*, Math. Comput. Modelling, **32**(2000), 1503-1528.
- [3] V. Ilea, D. Otrocol: *On the Burton method of progressive contractions for Volterra integral equations*, Fixed Point Theory, **21**(2020), no. 2, 585-594.
- [4] A. Petruşel, I.A. Rus: *On some classes of Fredholm-Volterra integral equations on spaces of functions on several variables*, Montes Taurus J. Pure Appl. Math. (in press).
- [5] A. Petruşel, I.A. Rus, M.A. Şerban: *Some variants of fibre contraction principle and applications: from existence to the convergence of successive approximations*, Fixed Point Theory, **22**(2021), no. 2, 795-808.
- [6] I.A. Rus: *Some variants of contraction principle in the case of operators with Volterra property: step by step contraction principle*, Adv. Theory of Nonlinear Anal. Appl., **3**(2019), no. 3, 111-120.
- [7] E.S. Zhukovskii, M.J. Alves: *Abstract Volterra operators*, Russian Math. (Iz. VUZ), **52**(2008), no. 3, 1-14.

On Some Concepts of Uniform Dichotomy for Evolution Operators in Banach Spaces

Sep 10
18:40-19:00

Rovana Boruga(Toma)¹, Mihail Megan², Daniela Maria-Magdalena Toth¹

¹West University of Timisoara/Department of Mathematics, Faculty of Mathematics and Computer Science, Timisoara, Romania

²Academy of Romanian Scientists, 050094 Bucharest, Romania,
West University of Timisoara/Departament of Mathematics, Faculty of Mathematics and Computes Science, Timisoara, Romania

Abstract: The paper presents three concepts of uniform dichotomy: uniform exponential dichotomy, uniform polynomial dichotomy and uniform dichotomy with growth rates for dynamical systems described by evolution operators in Banach spaces. Characterizations and connections between these concepts are given.

Keywords: evolution operators, uniform exponential dichotomy, uniform polynomial dichotomy, uniform dichotomy with growth rates.

MSC2010: 34D05, 93D20.

Recent Trends in Geometric Function Theory

Sep 11
9:00-9:40

Daniel Breaz¹

¹"1 Decembrie 1918" University of Alba Iulia, Romania

Abstract: We consider some new general integral operators which extend integral classical operators in geometric functions theory. Also, we prove some properties of univalence, starlike, convexity and other results for this operators.

Convergence Estimates for Some Two Parameters Singularly Perturbed Problems for Sine-Gordon Type Equations

Sep 11
9:40-10:00

Andrei Perjan¹, Galina Rusu¹

¹Department of Mathematics, Moldova State University, Chisinau, Republic of Moldova

Abstract: In the real Sobolev space $H_0^1(\Omega)$ we consider the Cauchy-Dirichlet problem for sine-Gordon type equation with strongly elliptic operators and two small parameters. Using some a priori estimates of solutions to the perturbed problem and a relationship between solutions in the linear case, we establish convergence estimates for the difference of solutions to the perturbed and corresponding unperturbed problems. We obtain that the solution to the perturbed problem has a singular behavior, relative to the parameters, in the neighbourhood of $t = 0$.

Keywords: Sine-Gordon type equation, singular perturbation, boundary layer function, a priori estimate.

MSC2010: 35B25, 35K15, 35L15, 34G10.

Acknowledgements. Researches supported by the Project 20.80009.5007.25.

References:

- [1] T.A. Burton: *A note on existence and uniqueness for integral equations with sum of two operators: progressive contractions*, Fixed Point Theory, **20**(2019), no. 1, 107-113.
- [2] C. Corduneanu: *Abstract Volterra equations: a survey*, Math. Comput. Modeling, **32**(2000), 1503-1528.
- [3] V. Ilea, D. Otrocol: *On the Burton method of progressive contractions for Volterra integral equations*, Fixed Point Theory, **21**(2020), no. 2, 585-594.
- [4] A. Petruşel, I.A. Rus: *On some classes of Fredholm-Volterra integral equations on spaces of functions on several variables*, Montes Taurus J. Pure Appl. Math. (in press).
- [5] A. Petruşel, I.A. Rus, M.A. Şerban: *Some variants of fibre contraction principle and applications: from existence to the convergence of successive approximations*, Fixed Point Theory, **22**(2021), no. 2, 795-808.
- [6] I.A. Rus: *Some variants of contraction principle in the case of operators with Volterra property: step by step contraction principle*, Adv. Theory of Nonlinear Anal. Appl., **3**(2019), no. 3, 111-120.
- [7] E.S. Zhukovskii, M.J. Alves: *Abstract Volterra operators*, Russian Math. (Iz. VUZ), **52**(2008), no. 3, 1-14.

On Well-posedness Associated With a New Class of Constrained Optimization Problems

Sep 11
10:00-10:20

Savin Treanță¹

¹University Politehnica of Bucharest, Department of Applied Mathematics, Bucharest, Romania

Abstract: In this paper, by using the notions of monotonicity, lower semicontinuity, pseudomonotonicity and hemicontinuity associated with the considered scalar multiple integral functional, we investigate well-posedness for a new class of control problems with variational inequality constraints. More precisely, by introducing the approximating solution set of the considered class of variational control problems, we formulate and prove several characterization results on well-posedness. Also, in order to highlight the theoretical results and tools derived in the paper, some illustrative examples are provided.

Keywords: well-posedness; well-posedness in the generalized sense; variational control problem; monotonicity; pseudomonotonicity; hemicontinuity; multiple integral functional.

MSC2010: 49K40; 65K10.

A Spectral Criterion for the Existence of the Stabilizing Solution of a Class of Riccati Type Differential Equations with Periodic Coefficients

Sep 11
10:20-10:40

Vasile Drăgan¹, Ioan-Lucian Popa²

¹Institute of Mathematics "Simion Stoilow" of the Romanian Academy, P.O.Box 1-764, RO-014700, Bucharest, Romania

and the Academy of the Romanian Scientists

²Department of Computing, Mathematics and Electronics, "1 Decembrie 1918" University of Alba Iulia, 510009 - Alba Iulia, Romania

Abstract: This talk is devoted to show the existence and uniqueness of a stabilizing solution to a periodic backward nonlinear differential equation. This class of nonlinear equations includes as special cases many of the continuous-time Riccati equations arising both in deterministic and stochastic linear quadratic type control problems.

Keywords: generalized Riccati equations; stabilizing solution; the periodic case; characteristic multipliers.

MSC2010: 49N10; 93E20

On A_n -bounded Operator Valued Analytic Functions

Sep 11
10:40-11:00

Ilie Valuşescu¹

¹Institute of Mathematics "Simion Stoilow" of the Romanian Academy (IMAR),
Bucharest, Romania

Abstract: For various purposes, scalar valued analytic functions was extended to vector valued, or operator valued analytic functions. Such a way, bounded operator valued analytic functions was extended to the class of L^2 -bounded operator valued analytic functions, to find a model for infinite variate prediction. In this paper the class of L^2 -bounded operator valued analytic functions, which generalized the class of bounded operator valued analytic functions $\{\mathcal{E}, \mathcal{F}, \Theta(z)\}$, is extended to the class of A_n -bounded operator valued analytic functions, or Bergman bounded analytic functions, to the aim of modeling the structure of n -hypercontractions in a similar mode which was made for contraction functional model in C_0 case. The functional model of a contraction in C_0 class given by the maximal function of the contraction is remembered, and a similar model for the case of n -hypercontractions is given with an attached maximal function which is actually an A_n -bounded operator valued analytic function on the unit disc \mathbb{D} .

Adaptive Gradient Descent and Slow Manifolds

Sep 11
11:30-11:50

Adrian Viorel¹

¹Department of Mathematics, Babeş-Bolyai University, Cluj-Napoca, Romania

Abstract: Recently, Y. Malitsky and K. Mishchenko have reignited the interest in classical gradient descent, albeit with variable step size, by proving that convergence rates can be obtained without assuming the global Lipschitz continuity of the objective function's gradient and thus, without an a priori condition on the step size. We build upon their ideas and show that the true power of adaptive step size gradient descent manifests itself in the presence of so called slow manifolds, along which the local flatness allows for larger and larger steps.

Keywords: gradient flows, gradient descent, slow manifolds, convex optimization.

MSC2010: 90C26, 90C30, 65K10.

Sep 11
11:50-12:10

On Some Exact Integral Formulae for Polynomial Coefficients and Enumeration of Multipartitions

Ovidiu Bagdasar¹

¹University of Derby, College of Science and Engineering, Derby, United Kingdom

Abstract: The Cauchy integral formula has numerous applications in various mathematics fields, including complex analysis, combinatorics, or number theory. Here we show how it can be used to derive exact formulae for the coefficients of cyclotomic polynomials and other classes of special polynomials. We also discuss applications to the enumeration of ordered multi-partitions with equal sum for multisets, where we present some recent additions to the Online Encyclopedia of Integer Sequences (OEIS).

MSC2010: 11B83, 05A15, 05A16, 05A18, 11B75.

References:

- [1] Andrica, D., Bagdasar, O., *On some results concerning the polygonal polynomials*, Carpathian J. Math., **35** (2019), 1–12.
- [2] Andrica, D., Bagdasar, O., *A new formula for the coefficients of Gaussian polynomials*, An. Șt. Univ. Ovidius Constanța **27**(3) (2019), 25–36.
- [3] Andrica, D., Bagdasar, O., *Remarks on a family of complex polynomials*, Appl. Anal. Discr. Math., **13** (2019), 605–618.
- [4] Andrica, D., Bagdasar, O.: *Recurrent Sequences: Key Results, Applications and Problems*. Springer (2020)
- [5] Andrica, D., Bagdasar, O., *On k -partitions of multisets with equal sums* The Ramanujan Journal, **55** (2021), 421–435.

Sep 11
12:10-12:30

The Determinant Formulae for the Rodrigues General Problem when the Eigenvalues Have Double Multiplicity

Dorin Andrica¹, Oana-Liliana Chender¹

¹Department of Mathematics, Babeș-Bolyai University Cluj-Napoca, Romania

Abstract:

Consider the analytic function f defined on the domain $D \subseteq \mathbb{C}$. If $X \in M_n(\mathbb{C})$ and $\sigma(X) \subset D$, then according to the Hamilton-Cayley-Frobenius theorem, we have the Rodrigues formula for the matrix $f(X)$

$$f(X) = \sum_{k=0}^{n-1} a_k^{(f)}(X) X^k,$$

where the numbers $a_0^{(f)}(X), \dots, a_{n-1}^{(f)}(X)$ are the Rodrigues coefficients of f with respect to the matrix X . The determination of the Rodrigues coefficients for a given analytic function is called *the Rodrigues general problem* (see [1]).

In the paper [2, Theorem 5] the Rodrigues general problem is completely solved when the eigenvalues $\lambda_1, \dots, \lambda_s$ of the matrix $X \in M_{2s}(\mathbb{C})$ are distinct and have double multiplicity. The main purpose of this present paper is to present, in this

case, a closed form for the Rodrigues coefficients by involving suitable determinants of order $n = 2s$.

References:

[1] D. Andrica, O.L. Chender (Broaina), *A New Way to Compute the Rodrigues Coefficients of Functions of the Lie Groups of Matrices* in "Essays in Mathematics and its Applications" in the Honor of Vladimir Arnold, Springer, 2016, 1-24.

[2] O.L. Chender (Broaina), *Computational Aspects of the General Rodrigues Problem* in "Mathematical Analysis in Interdisciplinary Research", I.N. Parasidis, E. Providas, Th. M. Rasiias, Eds., Springer Nature, 14 pp, to appear.

A Fractional Differential Inclusion with Mixed Boundary Conditions

Sep 11
12:30-12:50

Aurelian Cernea¹

¹Faculty of Mathematics and Computer Science, University of Bucharest, Romania

Abstract: A Caputo type fractional derivative of a function with respect to another function ([3]) that extends and unifies several fractional derivatives existing in the literature like Caputo, Caputo-Hadamard, Erdélyi-Kober was intensively studied in recent years. In particular, existence results and qualitative properties of the solutions for fractional differential equations defined by this fractional derivative are obtained in [1,2].

We extend the study to the set-valued framework and we consider the following problem

$$D_C^{\alpha,\psi} x(t) \in F(t, x(t)) \quad a.e. ([a, b]), \quad x(a) = x_0, \quad x'(0) = x_1, \quad x(b) = kI^{\alpha,\psi} x(c), \quad (1)$$

where $D_C^{\alpha,\psi}$ is the fractional derivative mentioned above, $\alpha \in (2, 3)$, $x_0, x_1, k \in \mathbf{R}$, $c \in (a, b)$ and $F : [a, b] \times \mathbf{R} \rightarrow \mathcal{P}(\mathbf{R})$ is a set-valued map which is Lipschitz in the state variable.

Our aim is twofold. On one hand, we show that Filippov's ideas can be suitably adapted in order to obtain the existence of solutions for problem (1) and on the other hand, we prove the arcwise connectedness of the solution set of problem (1).

Keywords: differential inclusion, selection, boundary value problem.

MSC2010: 34A60, 26A33, 34A08.

References:

[1] R. Almeida, *Fractional differential equations with mixed boundary conditions*, Bull. Malays. Math. Sci. Soc. 42 (2019), 1687-1697.

[2] R. Almeida, A.B. Malinowska, M.T.T. Monteiro, *Fractional differential equations with a Caputo derivative with respect to a kernel function and their applications*, Math. Meth. Appl. Sci 41 (2018), 336-352

[3] A.A. Kilbas, H.M. Srivastava, J.J. Trujillo, *Theory and Applications of Fractional Differential Equations*, Elsevier, Amsterdam, 2006.

The Hardy-Littlewood-Pólya Inequality of Majorization in the Context of Ordered Banach Spaces

Sep 11
14:00-14:40

Constantin P. Niculescu¹

¹University of Craiova, Romania

Abstract: The Hardy-Littlewood-Pólya inequality of majorization is extended to the framework of ordered Banach spaces. Our main result deals with Gâteaux differentiable convex functions whose differentials are isotone (that is, order preserving). Then the conclusion is extended to a nondifferentiable framework involving convex functions defined on open N -dimensional intervals of \mathbb{R}^N , which verify a condition of monotonicity à la Popoviciu (called by us 2-box monotonicity). Several applications illustrating our findings are also included.

Numerical Probabilistic Analysis of a Generalized Random Logistic Model

Sep 11
14:40-15:00

Vicente Bevia¹, Juan Carlos Cortés¹

¹Instituto de Matemática Multidisciplinar, UPV, Valencia, Spain

Abstract: Consider the following initial value problem (IVP) based on a non-autonomous ordinary differential equation

$$\dot{N}(t) = \alpha(t) r N(t) \left(1 - \left(\frac{N(t)}{K} \right)^\nu \right), \quad t > 0, \quad (1)$$

$$N(0) = N_0. \quad (2)$$

This type of equation can model a great variety of growth processes [1] due to the fact that it can account for a time-dependent lag phase ($0 \leq \alpha(\cdot) \leq 1$, [2]) after which it has a logistic-type growth, as well as a deceleration parameter (ν) which affects the time at which growth speed begins to decay. The remaining parameters have the same meaning as in the usual logistic model: $r > 0$ is the initial growth rate, $K > 0$ is the asymptotic state of the system, $N(t)$ is the state at time $t \geq 0$ and N_0 is the initial state of the model.

In this contribution we will give a density-based probabilistic analysis of the IVP (1)–(2) with random initial condition and random parameters. The probability density function is obtained by solving the Liouville-Gibbs partial differential equation [3] using numerical simulation techniques such as Lagrangian methods and Adaptive Mesh Refinement. Finally, all the aforementioned theoretical results will be applied to a real data-set of a biological culture growth [4].

Keywords: Randomness, Density Function, Numerical methods, Optimization.

MSC2010: 34D09.

References:

[1] Tjørve KMC and Tjørve E, The use of Gompertz models in growth analyses, and new Gompertz-model approach: An addition to the Unified-Richards family. *PLOS ONE* 12(6): e0178691, 2017

[2] Baranyi, J., and Roberts, T. A., A dynamic approach to predicting bacterial growth in food. *International journal of food microbiology*, 23(3-4), 277-294, 1994.

[3] Soong, T.T., Random Differential Equations in Science and Engineering. New York and London, Academic Press, 1974.

[4] Ram, Y., Dellus-Gur, E., Bibi, M., Karkare, K., Obolski, U., Feldman, M.W., Cooper, T.F., Berman, J. and Hadany, L., Predicting microbial growth in a mixed culture from growth curve data. *Proceedings of the National Academy of Sciences*, 116(29), 14698–14707, 2019.

On Some Concepts of Uniform Dichotomy for Evolution Operators in Banach Spaces

Sep 11
15:00-15:20

Timea Melinda Szemely Fülöp¹, Ariana Găină², Carmen Florinela Popa¹

¹West University of Timisoara/Department of Mathematics, Faculty of Mathematics and Computer Science, Timisoara, Romania

Abstract: In this paper, we investigate a more general concept of uniform stability for linear discrete-time systems in Banach spaces. This concept includes as particular cases the concepts of uniform exponential stability and uniform polynomial stability. For these concepts we obtain five characterization-types.

Keywords: Linear discrete-time stability, uniform h-stability, uniform exponential stability, uniform polynomial stability.

MSC2010: 34D05.

Maia's Fixed Point Theorems for Discontinuous Mappings

Sep 11
15:20-15:40

Paula Mihaela Tamara Homorodan¹

¹Technical University of Cluj-Napoca North University Center at Baia Mare, Romania

Abstract: We establish new fixed point theorems for Maia's fixed point theorem in the setting of a space with a distance, more precisely when both metrics are replaced with two distance. We also indicate some particular cases of our main results and present some examples to illustrate the theoretical results and show that our generalizations are effective.

Keywords: Space with distance, H -distance space, partially ordered, Kannan type mappings, Bianchini type mappings.

MSC2010: 47H10; 47H09.

Sep 11
15:40-16:00

Torsional Creep Problems Involving Grushin p -Laplacian

Denisa Stancu-Dumitru¹

¹Department of Mathematics and Computer Sciences, University Politehnica of
Bucharest, Romania

Abstract: The asymptotic behaviour of solutions for a family of torsional creep problems involving the Grushin p -Laplace operator is analyzed. In particular, our results complement some earlier works on the topic by L. E. Payne & G. A. Philippin [3], B. Kawohl [2] and T. Bhattacharya, E. DiBenedetto and J. Manfredi [1]. This is based on a joint work with Mihai Mihăilescu. This presentation is partially supported by CNCS-UEFISCDI Grant No. PN-III-P1-1.1-TE-2019-0456.

Keywords: Torsional creep problems; Grushin p -Laplacian; weak solutions; compact embeddings; Γ -convergence.

MSC2010: 35D30; 46E30; 46E35; 49J45; 49S99.

References:

[1] T. Bhattacharya, E. DiBenedetto, & J. Manfredi: Limits as $p \rightarrow \infty$ of $\Delta_p u_p = f$ and related extremal problems, *Rend. Sem. Mat. Univ. Politec. Torino*, special issue (1991), 15-68.

[2] B. Kawohl: On a family of torsional creep problems, *J. Reine Angew. Math.* **410** (1990), 1-22.

[3] L. E. Payne & G. A. Philippin: Some applications of the maximum principle in the problem of torsional creep, *SIAM J. Appl. Math.* **33** (1977), 446-455.

Sep 11
16:00-16:20

On Coupled Nonlinear Oscillators of a Mechanical System of Vibration Reduction

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Abstract: We investigate nonlinear systems of second order ODEs describing the dynamics of two coupled nonlinear oscillators of a mechanical system of vibration reduction. We obtain, under certain assumptions, some stability results for the null solution. Also, we show that, in the presence of a time dependent external force, every solution starting from initial data small enough is bounded or goes to zero as time tends to infinity, provided that suitable conditions are satisfied. Our theoretical results are illustrated with numerical simulations.

Keywords: coupled oscillators, uniform stability, asymptotic stability, uniform asymptotic stability, vibration reduction.

MSC2010: 34D20.

Dynamics of the Infection by SARS-CoV-2

Sep 11
16:20-16:40

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Abstract: This paper adapts the Susceptible-Infected-Quarantined-Recovered model (aSIQR) for describing the dynamics of the SARS-CoV-2 virus propagation, responsible for the COVID-19 pandemic. Numerical results are shown for Portugal (PT), United States (US), and France (FR). There is a good agreement of the simulations and the data available for these countries.

Unbounded Solutions of Third Order Three-point Boundary Value Problems on a Half-line

Sep 11
16:40-17:20

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Abstract: We consider the following third order three-point boundary value problem on a half-line

$$\begin{aligned}x'''(t) + q(t)f(t, x'(t), x''(t)) &= 0, \quad t \in (0, \infty), \\x'(0) = A, \quad x(\eta) = B. \quad x''(+\infty) &= C,\end{aligned}$$

where $\eta \in (0, +\infty)$, but fixed, and $f : [0, +\infty) \times \mathbb{R}^3 \rightarrow \mathbb{R}$ satisfies Nagano's condition. We apply Schauder's fixed point theorem, the upper and lower solution method, and topological degree theory, to establish the existence theory for at least one unbounded solution, and at least three unbounded solutions. To demonstrate the usefulness of our results we illustrate two examples.

Author Index

- Adrian Petrușel, 7
Adrian Viorel, 11
Andrei Perjan, 9
Ariana Găină, 15
Aurelian Cernea, 13
- Carla M.A. Pinto, 17
Carmen Florinela Popa, 15
Constantin P. Niculescu, 14
Cristian Vladimirescu, 16
- Daniel Breaz, 8
Daniela Maria-Magdalena Toth, 8
Denisa Stancu-Dumitru, 16
Dorin Andrica, 12
Dumitru Băleanu, 7
- Galina Rusu, 9
Gheorghe Moroșanu, 16
Ilie Valușescu, 11
- Ioan-Lucian Popa, 10
- Juan Carlos Cortés, 14
- Mihail Megan, 8
- Oana-Liliana Chender, 12
Ovidiu Bagdasar, 12
- Paula Mihaela Tamara Homorodan,
15
- Ravi P. Agarwal, 17
Rovana Boruga(Toma), 8
- Savin Treanță, 10
- Timea Melinda Szemely Fülöp, 15
- Vasile Drăgan, 10
Vicente Bevia, 14